

# A Collusion Attack on Pairwise Key Presdistribution Schemes for Distributed Sensor Networks

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# Introduction

- Key predistribution schemes considered the **safest** way to bootstrap trust in a sensor network
- Main drawback: **high storage overhead**
- Key predistribution can actually be quite **insecure**
  - Many pre-loaded global secrets strengthen attacker incentive
  - Localised communication helps hide misbehaviour
- We describe an attack where colluding nodes reuse selected pairwise keys to create many false identities and hijack majority of communications

# Bootstrapping a sensor network

- Constraints for establishing secure communication
  - Sensors deployed in hostile environments  $\Rightarrow$  global passive adversary
  - No tamper-resistant hardware  $\Rightarrow$  several corrupt nodes
  - Network topology unknown prior to deployment
  - No access to centralised server, trusted third party, etc.
- Solution
  - Assign keys to nodes in advance
  - Must balance security against storage and computing limitations of sensors

# Options for predistributing keys

- Single master key predistribution
  - Inexpensive but susceptible to single compromise
- Pairwise key predistribution
  - Resilient to widespread compromise but storage infeasible for large networks (requires  $n - 1$  keys per node)
- Random key predistribution (Eschenauer & Gligor CCS 2002)
  - Nodes are assigned a random subset of keys from a large key space
  - If nodes share a common key, then a link can be established
  - Probabilistic guarantees based on random graph theory
  - Efficient, though fails badly when a small group of nodes are compromised

## Options for predistributing keys (ctd.)

- Random pairwise scheme (Chan *et al.* IEEE S&P 2003)
  - Combines the random graph approach with pairwise key assignment
  - More efficient than pure pairwise scheme, but requires much more storage than EG 2003 (each node typically stores between  $0.2n$  and  $0.4n$  keys, depending on parameters)
  - No duplicate keys, so secure against eavesdropping attacks
  - Authors claim that pairwise key assignment enables mutual authentication at no added cost
- But is it secure from a colluding attacker?

# Notation and system parameters

- Notation
  - $n$ : Network size
  - $n'$ : **expected** number of neighbour nodes in radio range
  - $p$ : probability of two nodes sharing a pairwise key
  - $N(d)$ : set of neighbours of node  $d$
  - $U(d)$ : set of usable pairwise keys for node  $d$
- System model
  - Nodes have limited communication radius
  - Nodes distributed uniformly across a space
  - Nodes pre-loaded with  $n * p$  pairwise keys
  - Nodes broadcast their identifiers to neighbours, who check ID to see if they share a pairwise key

# Attack preconditions

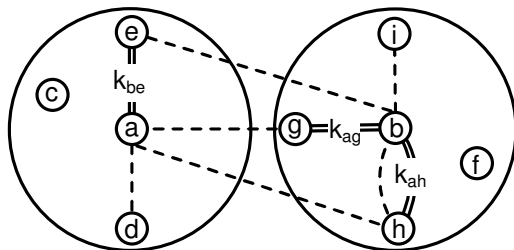
- Threat model
  - Attacker compromises a set of nodes  $A$ ,  $q = |A|$ , obtaining keys and controlling all communications
  - Attacker nodes may collude across network via existing routing mechanism or an out-of-band channel
  - Attack targets the integrity and availability of communications
- Weaknesses of key predistribution
  - Many more secrets pre-loaded than actually used for communication ( $n * p \gg n'$ )
  - Sensors have localised interactions, but global key assignment
- **Key insight:** colluding attackers can exploit latent secrets and communication gaps

## Attack description

- Consider two nodes controlled by an attacker,  $a, b \in A$ 
  - $a$  tells  $b$  its secrets
  - $b$  masquerades as  $a$  to all of  $b$ 's neighbours that  $a$  shares a pairwise key with, and vice versa
  - Repeat for all pairs of nodes in  $A$
- As more nodes are compromised, more keys can be reused
- Like a Sybil attack (each node presents multiple identities)
- Like a node replication attack (multiple copies of same node)
- Attacker nodes pretend to be different nodes to different neighbours



# Example attack

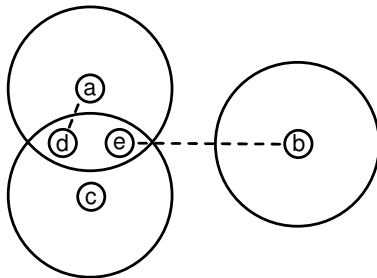


----- legitimate pairwise key  
 == $k_{ag}$ == colluding pairwise key

	Independence	Collusion
$U(a)$	$\{k_{ad}\}$	$\{k_{ad}, k_{be}\}$
$U(b)$	$\{k_{bh}, k_{bi}\}$	$\{k_{bh}, k_{bi}, k_{ag}, k_{ah}\}$



# Overlap



- Only one of nodes  $a$  and  $c$  should masquerade as  $b$  to node  $e$
- Node  $c$  gains nothing by pretending to be  $a$  to  $d$
- Overlap unavoidable as  $q \rightarrow \frac{n}{n'}$

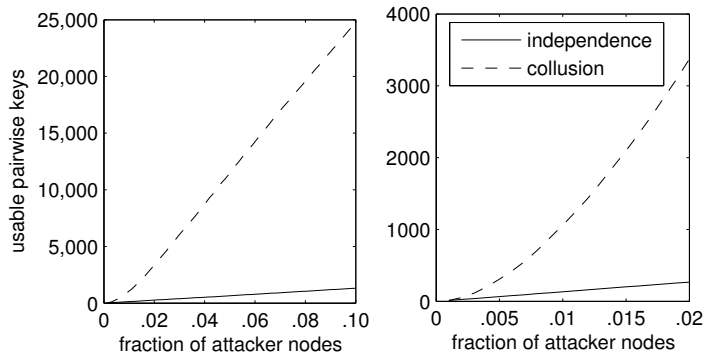
# Attack Discussion

- Integrity, availability of communications targeted, **not** confidentiality
  - Many false channels can overwhelm legitimate ones
  - Authentication based on pairwise key possession inadequate
  - Node revocation, redundant routing schemes undermined
- Attack variables
  - **Coordination levels**: ratio  $\frac{n'}{n}$  between average node neighbourhood and network size
  - **Key storage**: as  $p$  increases, more secrets can be exploited

# Impact Analysis & Measurement

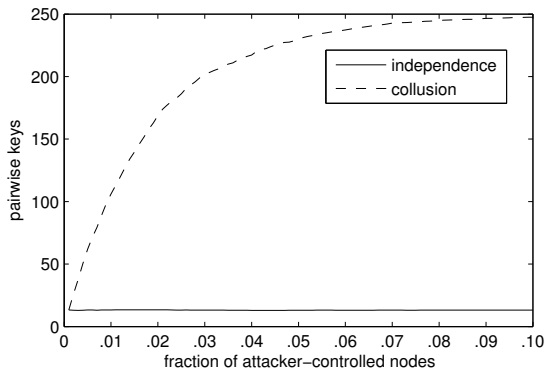
- We focus on the number of **usable** pairwise secret keys available to an attacker
  - A pairwise key is **usable** if it is shared between nodes in communication range **and** it is not already in use within this range
- Attack Metrics
  - Number of usable pairwise keys available to a colluding attacker
  - Ratio of usable keys for attacker to keys available to attacker's neighbours
- Simulations
  - Nodes uniformly distributed over a plane
  - $n = 1000$ ,  $n' = 60$ ,  $p = .25$  and varied  $q$ , averaging results from 20 rounds

## Increased usable pairwise keys



Measures  $\sum_{a \in A} |U(a)|$  for increasing  $q$

## Per-node usable pairwise keys



As  $q$  grows large, each colluding node can establish  $n * p$  fake communication channels



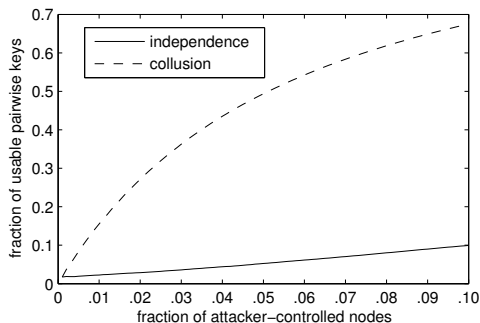
## Quantifying attacker penetration

- But what is the overall impact of a collusion attack?

$$I(A) = \frac{\sum_{a \in A} |U(a)|}{\sum_{a \in A} \sum_{b \in N(a)} |U(b)|}$$

- $I(A)$  compares the number of usable pairwise keys **available to an attacker** to the keys available to attacker-controlled nodes' **neighbours**
- $I(A)$  reveals the fraction of working communication channels controlled by the attacker

## Quantifying attacker penetration (ctd.)



- Corrupting 5% of nodes grants power to half of communication channels
- Any application requiring honest interaction with majority of neighbours is susceptible



## Storage requirements

- How can colluding nodes actually store extra keys?
  - $n * p$  keys pre-distributed
  - Up to  $n * p$  additional keys from collusion
  - Storing twice as many keys is too onerous
- Attack optimisation
  - Pairwise keys can only be used once by definition
  - After a node shares a pairwise key with another attacker-controlled node, it can delete the key and replace it with keys from the other node
  - So **key-sharing** becomes **key-swapping**
  - Attacker nodes still store no more than  $n * p$  keys

# Countermeasures

- Reduce value of compromised nodes to attackers
  - Discard unused keys after initialisation phase
    - No new nodes may join after initialisation
  - Reduce the number of pre-loaded keys
    - Exploit geographical proximity (topology foreknowledge)
    - Key infection (weaker attacker model)
- Detection mechanisms
  - Count connected neighbours
    - For normal usage, should share keys with  $n' * p$  neighbours
    - Attacked node may have up to  $q * p$  more
    - Identifying which neighbours are lying is difficult
  - Require nodes to transmit locations
    - Key reuse may be detected if nodes recursively ask neighbours for nodes' locations (Parno *et al.* 2005)
    - Location broadcast identifies new targets
    - Significant storage and transmission costs

# Conclusions

- We have presented a **collusion attack** on the class of pairwise key predistribution schemes
- Small fraction of compromised nodes required to control majority of communication channels
- We question the wisdom of assigning **global secrets** to **locally-communicating nodes**
- More research is needed for pairing limited secrets to localised interactions
- For more, visit <http://www.cl.cam.ac.uk/~twm29/>