

A brief introduction to economics

Part I

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Lecture 4

Notes

Key notions
Preferences
Utility
Expected utility

Motivation
Models

Why again are we studying economics?

- Economics is a *social science*
 - Studies behavior of individuals and firms in order to predict outcomes
 - Models of behavior based on systematic observation
 - Usually cannot run experiments as in bench science, but economics has developed ways to cope with differences inherent to observing the world
- Economics studies trade-offs between conflicting interests
 - Recognizes that people operate *strategically*
 - Have devised ways to model people's interests and decision making

3 / 44

Notes

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Economics is not just about money

- Money helps to reveal preferences
- Money can serve as a common measure for costs and benefits
- As a discipline, economics examines much more than interactions involving money
 - Economics studies trade-offs between conflicting interests
 - Conflicting interests and incentives appear in many circumstances where money never changes hands

4 / 44

Notes

Key notions
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Expected utility

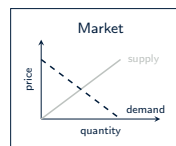
Motivation
Models

Notion of Model



Reality

Simplification
by projection



Model

- All models are wrong.
- Some are useful.

5 / 44

Notes

Occam's Razor



William of Occam, 1285–1349

*entia non sunt multiplicanda
praeter necessitatem*

*entities must not be
multiplied beyond
necessity*

10 / 44

Notes

Our first model: rational choice theory

- Economics attempts to model the *decisions* we make, when faced with multiple choices and when interacting with other strategic agents
- Rational choice theory (RCT): model for decision-making
- Game theory (GT): extends RCT to model strategic interactions

12 / 44

Notes

Rationality defined

- Intuitive definition: a **rational** individual acts in his or her perceived best interest
- Rationality is what motivates a focus on *incentives*
- Question: can you think of scenarios when this definition does not hold in practice?
- To arrive at a precise definition: use rational choice theory to state available outcomes, articulate preferences among them, and decide accordingly

13 / 44

Notes

Model of preferences

- An agent is faced with a range of possible outcomes $o_1, o_2 \in \mathcal{O}$, the set of all possible outcomes
- Notation
 - $o_1 \succ o_2$: the agent is strictly prefers o_1 to o_2 .
 - $o_1 \succeq o_2$: the agent weakly prefers o_1 to o_2 ;
 - $o_1 \sim o_2$: the agent is indifferent between o_1 and o_2 ;
- Outcomes can be also viewed as tuples of different properties $\hat{x}, \hat{y} \in \mathcal{O}$, where $\hat{x} = (x_1, x_2, \dots, x_n)$ and $\hat{y} = (y_1, y_2, \dots, y_n)$

14 / 44

Notes

From preferences to utility

- It's great to express preferences, but to make mathematical analysis of decisions possible, we need to transform these preferences into numbers.
- We need a measure of utility, but what does that actually mean?

20 / 44

Notes

We do not mean utility according to Bentham

- Founder of utilitarianism:
 "fundamental axiom, it is the greatest happiness of the greatest number that is the measure of right and wrong"
- Utility: preferring "pleasure" over "pain"



Jeremy Bentham

21 / 44

Notes

Utility

Rational choice theory defines utility as a way of quantifying consumer preferences

Definition

(Utility function) A utility function U maps a set of outcomes onto real-valued numbers, that is, $U: \mathcal{O} \rightarrow \mathbb{R}$. U is defined such that $U(o_1) > U(o_2) \iff o_1 \succ o_2$.

Agents make a rational decision by picking the outcome with highest utility:

$$o^* = \arg \max_{o \in \mathcal{O}} U(o) \quad (1)$$

22 / 44

Notes

Example utility functions

- $U(o_1, o_2) = u \cdot o_1 + v \cdot o_2$
 - Useful when outcomes are *substitutes*
 - Example substitutes: processor speed and RAM
- $U(o_1, o_2) = \min\{u \cdot o_1, v \cdot o_2\}$
 - Useful when outcomes are *complements*
 - Example complements: operating system and third-party software

23 / 44

Notes

Returning to our crypto example

- First, we need a utility function
 - $U(a_i, c_i) = u \cdot a_i + v \cdot c_i$
 - Question: why is this a good choice?
- For simplicity, we assign $a_{\oplus} = 1$, $a_{\ominus} = -1$, $c_{\oplus} = 1$, and $c_{\ominus} = -1$
- Utility is in the eye of the beholder
- We consider two scenarios
 - Intelligence agency ($u = 1$ and $v = 3$)
 - First responders ($u = 3$ and $v = 1$)

24 / 44

Utility of different outcomes

Outcome	U_{FR} (first responder)	U_{intel} (intelligence)
(a_{\oplus}, c_{\oplus})	4	4
$(a_{\oplus}, c_{\ominus})$	2	-2
$(a_{\ominus}, c_{\oplus})$?	?
$(a_{\ominus}, c_{\ominus})$?	?

25 / 44

Why isn't utility theory enough?

- Only rarely do actions people take directly determine outcomes
- Instead there is uncertainty about which outcome will come to pass
- More realistic model: agent selects action a from set of all possible actions \mathcal{A} , and then outcomes \mathcal{O} are associated with probability distribution

27 / 44

Lotteries

Definition

(Lottery) A lottery is a mapping from all outcomes $(o_1, o_2, \dots, o_n) \in \mathcal{O}$ to probabilities corresponding to each outcome (p_1, p_2, \dots, p_n) , where $\sum_{i=1}^n p_i = 1$. A lottery l_1 is represented as $l_1 = \langle o_1 : p_1, o_2 : p_2, \dots, o_n : p_n \rangle$.

28 / 44

Notes

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Where does randomness come from?

- Indeterminism in nature
- Lack of knowledge
- Incompleteness in the model
- Uncertainty concerns *which outcome* will occur
 - ⇒ Known unknowns, NOT unknown unknowns

29 / 44

Expected utility

Definition

(Expected utility (discrete)) The *expected utility* of an action $a \in \mathcal{A}$ is defined by adding up the utility for all outcomes weighed by their probability of occurrence:

$$E[U(a)] = \sum_{o \in \mathcal{O}} U(o) \cdot P(o|a) \quad (2)$$

Agents make a rational decision by maximizing expected utility:

$$a^* = \arg \max_{a \in \mathcal{A}} E[U(a)] \quad (3)$$

30 / 44

Example: process control system security

Global Exposure Surface Timeline

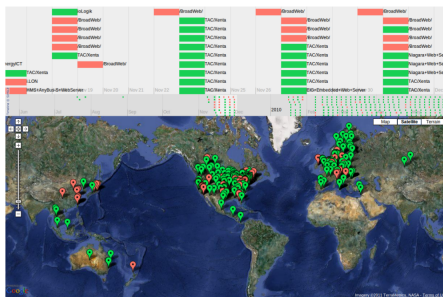


Figure 2.1: Example exposure time-map with red marking systems with known exploits

Source: <http://www.cl.cam.ac.uk/~fms27/papers/2011-Leverett-industrial.pdf>

31 / 44

Example: process control system security

- Actions available: $\mathcal{A} = \{\text{disconnect}, \text{connect}\}$
- Outcomes available: $\mathcal{O} = \{\text{attack}, \text{no attack}\}$
- If systems are connected, then the probability of successful attack is 0.01 ($P(\text{attack}|\text{connect}) = 0.01$)
- If systems are disconnected, then $P(\text{attack}|\text{disconnect}) = 0$

32 / 44

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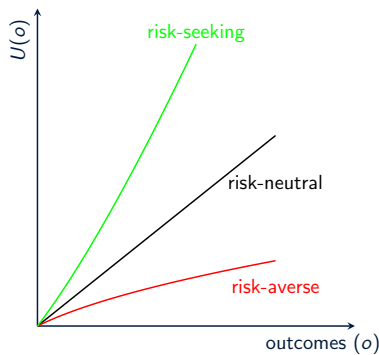
Let's make a deal (round 3)

- Option 1: Take \$10
- Option 2: Get \$50 with a 10% chance, \$0 otherwise
- Which would you choose?
- $E[U] = 0.1 * \$50 + 0.5 * \$0 = \$5$
- Prefer option 1: you're risk-averse or risk-neutral
- Prefer option 2: you've got a gambling problem

37 / 44

Notes

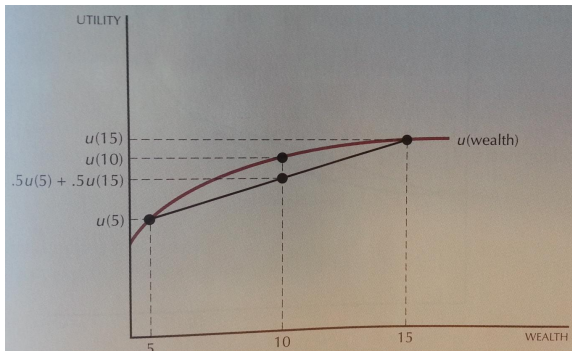
Risk attitudes depend on the behavior of the utility function



38 / 44

Notes

Risk-averse prefer utility of expected value over lottery

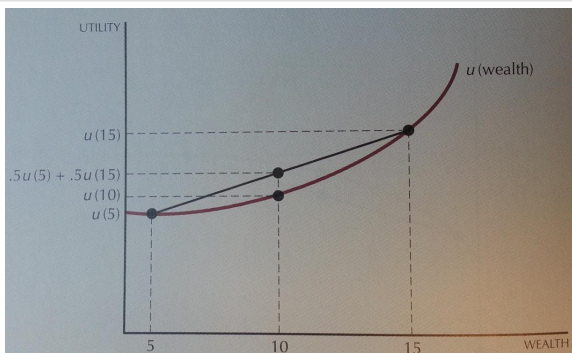


Source: Varian, *Intermediate Microeconomics*, p. 225

39 / 44

Notes

Risk-seekers prefer lottery over utility of expected value



Source: Varian, *Intermediate Microeconomics*, p. 226

40 / 44

Notes

From attitudes to utility

- Suppose that outcomes are numeric $\mathcal{O} \in \mathbb{R}$
- When might that happen?
- Then we can define risk-attitudes by how the utility function behaves

Definition

(Risk neutrality) An agent is risk-neutral when $U(o)$ is a linear function on o .

41 / 44

From attitudes to utility

Definition

(Risk aversion) An agent is risk-averse when $U(o)$ is a concave function (i.e., $U''(x) < 0$ for a twice-differentiable function).

Definition

(Risk seeking) An agent is risk-seeking when $U(o)$ is a convex function (i.e., $U''(x) > 0$ for a twice-differentiable function).

42 / 44

Example: antivirus software

- Suppose you have \$10,000 in wealth. You have the option to buy antivirus software for \$75.
- Outcomes available:

$$\mathcal{O} = \{\text{hacked (decreases wealth by \$2,000), not hacked (no change in wealth)}\}$$
- Without AV software, probability of being hacked is 0.05 ($P(\text{hacked}|\text{no antivirus}) = 0.05$)
- With AV software, probability of being hacked is 0 ($P(\text{hacked}|\text{antivirus}) = 0$)
- Exercise: compute the expected utility of both buying and not buying AV if you are risk-neutral (so that $U(o) = o$). Would you buy AV software?

43 / 44

Example: antivirus software

What if you are risk-averse (so that $U(o) = \sqrt{o}$)?

Risk-averse Action	hack		no hack		$E[U(\text{action})]$
	U	$P(\text{hack} \text{action})$	U	$P(\text{no hack} \text{action})$	
buy AV	$\sqrt{9,925}$	0	$\sqrt{9,925}$	1	99.6
don't buy	$\sqrt{8,000}$	0.05	$\sqrt{10,000}$	0.95	99.4

Exercise (on your own): How much would you pay for antivirus software if you were risk-neutral and the probability of getting hacked is 0.1 if you don't have AV installed?

44 / 44

Notes

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